Single-Phase Induction Motor with an Electronically Controlled Capacitor

Terrance A. Lettenmaier, Donald W. Novotny, Fellow, IEEE, and Thomas A. Lipo, Fellow, IEEE

Abstract—A single-phase induction motor using a new electronically controlled capacitor is described. The system uses a dc capacitor switched by a transistor H bridge. By proper control of the transistor switching, the circuit synthesizes a continuously variable capacitance in series with the auxiliary winding. The system could be used to replace standard single-phase motor capacitor configurations to provide improved machine performance. Basic system operation, a comparison with conventional motor operation, and illustrations of some of the design flexibility inherent in the new system are included.

INTRODUCTION

STANDARD capacitor-run single-phase induction motors use a capacitor in series with an auxiliary winding to produce a starting torque and to enhance running performance. These systems have the disadvantage that the capacitor size required for proper system operation is large at locked rotor and much smaller at full speed. To overcome this problem, a large capacitor is often centrifugally switched open before the operating speed is reached to give the desired performance. Although this switching provides different capacitor values in two speed ranges, improved machine performance requires the capacitance to be continuously varied. An alternative approach, which uses electronic switching to replace the centrifugal switch and to supply a continuously variable capacitance to the machine, is described in this paper.

The intent of the paper is to demonstrate the technical feasibility of the proposed system and to illustrate some of the design tradeoffs that are possible. After a description of the basic system, a comparison with a normal capacitor-run motor is presented. The effects of independent adjustments in several system parameters are then considered, and the circuit device requirements are described. Both analog and digital simulations are used to carry out the analysis.

SYSTEM DESCRIPTION

The major distinguishing feature of this system is a dc-charged capacitor switched by a transistor H bridge. A schematic of the electronically switched system, including the switching modulation scheme, is given in Fig. 1. The H bridge is pulse-width modulated using the sine-triangle modulation algorithm with a switching frequency of 1 kHz. The capacitor is charged with a dc voltage, obtained from the motor ac supply, and may be of the electrolytic type.


© 1991 IEEE

Fig. 1. Capacitor bridge run motor and switching modulation scheme.

The transistor switching is controlled by using the machine source voltage $V_s$ as a reference for the modulation. The modulation voltage $V_{ref}$ is synchronized and is phase-adjustable in relation to $V_s$. With a large enough capacitor, the voltage $V_{cap}$ is dc with no appreciable ripple; therefore, the bridge output $V_{br}$ is a pulse-width modulated approximation to a sine wave with a fundamental component phase adjustable in relation to $V_s$. The phase angle between $V_{br}$ and $V_s$ is called the “bridge phase” and is the primary adjustment used to control the transistor switching. By controlling the switching in this manner, the bridge output synthesizes a capacitance that may be varied by adjustment of the bridge phase. The size of the dc capacitor in the bridge need only be large enough to control the ac ripple at the capacitor terminals.

A secondary adjustment used to control the transistor switching is the magnitude of the modulation reference voltage $V_{ref}$ in relation to the triangle wave peak $V_t$. This ratio is called the modulation scale factor and is symbolized by “$a$.” As will be shown, the effect of this adjustment is to change the dc voltage of the capacitor $V_{cap}$ in relation to the fundamental voltage at the bridge output.

Theory of Operation

Under steady-state conditions, the capacitor bridge-run machine operates in the same way as a capacitor-run motor with a variable capacitance. The capacitor bridge circuit supplies an “effective” ac capacitance to the machine, which may be changed by adjusting the bridge phase. First consider the machine running in a steady-state condition. The capacitor bridge...
circuit only has switches and an energy storage element (the capacitor) and can neither absorb nor generate average power. For this reason, the auxiliary current $I_{aux}$ must lead or lag the bridge voltage $V_{br}$ by 90°. Because the energy storage element in the bridge is a capacitor, $I_{aux}$ leads $V_{br}$, and the bridge acts as a capacitor. Because the capacitor bridge output is capacitive and the phase of the bridge output voltage may be set in relation to the main winding voltage $V_{m}$, steady-state operation can be related to that of a standard capacitor-run motor.

A capacitor-run motor in any steady-state condition has a unique capacitor voltage magnitude and phase angle. A change in capacitor size will give a different voltage magnitude and phase at the same motor speed. From a conceptual point of view, the two capacitor constraints (i.e., the fixed ratio of capacitor voltage and current and the 90° phase relationship) combined with the motor constraint equations determine the unique operating point.

In the capacitor bridge-run motor, there is also a capacitive element in the circuit as a result of the 90° relation between the bridge voltage and the auxiliary current. However, the second constraint is on the bridge phase angle, as set by the modulation phase angle, rather than on the ratio of amplitudes as in a capacitor. These two constraints (i.e., the phase of the bridge voltage with respect to the source and the 90° phase relationship between bridge voltage and auxiliary current) are sufficient to uniquely determine the operating point. In effect, there is only one possible voltage magnitude and “effective capacitance” at the bridge output, and the dc capacitor voltage must adjust itself to provide the required bridge voltage.

Thus, the basic mode of operation is to use the phase of the voltage reference for the switching modulation to control the effective capacitance of the bridge. Because the bridge voltage is fixed by machine constraints for any particular bridge phase, changes in the modulation ratio “a” cannot change $V_{br}$. Instead, changing “a” only changes the ratio of $V_{cap}$ to $V_{br}$, which in turn changes $V_{cap}$. The modulation ratio can therefore be used to control the dc capacitor voltage but will have no direct influence on steady-state machine performance.

Analyzing the capacitor bridge-run machine as a capacitor-run machine with a variable capacitor, optimal operation of the system can be explored. Under any start or run condition, there is some value of capacitance that will give the motor the best torque output, running efficiency, or other desirable property. If this value of capacitance is known for all machine conditions, the phase of $V_{cap}$ can be adjusted to give the proper effective capacitance at all times. With this adjustment, the motor will run optimally under every condition.

Under a transient condition where either the machine operating condition or bridge switching modulation is changed, the dc capacitor must charge or discharge to a new voltage. Under this transient condition, the bridge circuit either absorbs or delivers average power and is no longer completely capacitive. Therefore, the auxiliary current does not lead the bridge voltage by 90°. The duration of this transient condition depends on the size of dc capacitor used. However, the capacitor voltage can be controlled by the modulation scaling factor “a.” With proper control of “a,” $V_{cap}$ can be kept constant through any transient operation of the motor, and the bridge always acts as a capacitive element in the system.

SIMULATION METHODS

The basis for all simulation was the 1/3-hp capacitor-run motor with ratings and parameters shown in Table I. Simulations were performed in which the ac run capacitor was replaced by the capacitor bridge circuit. Initially, an analog computer was used for exploratory evaluation of the circuit. Subsequently, the capacitor bridge-run motor was verified as equivalent in the steady state to a standard capacitor-run motor with an adjustable capacitance. A digital computer simulation of the capacitor run motor was used for steady state analysis by using the run capacitor size as a variable. The results of the analog and digital simulations matched closely and both are used here.

Both simulations were based on a standard d-q axis model of a symmetrical two-phase induction machine in the stationary reference frame [2]. The symmetrical two-phase machine was modified by a step-up transformer on the $d$ axis to give a nonunity auxiliary to main winding turn ratio. The motor parameters were modified to give both windings of the symmetrical machine identical leakage reactance and resistance values for simplicity, corresponding to equal wire bulk for both windings of the capacitor-run motor.

The simulations were run in either an adjustable torque mode to simulate steady-state machine operation or an adjustable-speed mode to analyze starting conditions. Although the analog computer was capable of transient simulation for the starting condition, detailed analysis was made with the motor speed set to different points in the starting curve to analyze changes in the transistor switching algorithm easily. This approach assumes that the capacitor voltage is controlled to be constant during machine transients.

SYSTEM PERFORMANCE

To illustrate the type of control that can be achieved, the performance of the capacitor bridge run machine is now compared with the performance of the standard 5-$\mu$F capacitor-run machine. The capacitor bridge-run machine was simulated with a large dc capacitor of 100 $\mu$F and the bridge phase adjusted for “optimal” performance at each operating point. The maximization of the average torque is considered to be optimal for the start conditions and the minimization of the pulsating torque optimal for the run conditions.

Speed-Torque Curve

Fig. 2 shows the average torque versus speed plots for the bridge-run machine and capacitor-run machine. The bridge phase of the bridge-run machine was adjusted at each speed to maximize the average torque output. The capacitor bridge machine has a greater torque output at all speeds. As expected, the different is large at low speeds, where the run capacitor is far too small; the locked rotor torque for the capacitor bridge machine is 3.5 Nm compared with 0.5 Nm for the capacitor-run machine. The breakdown torque is about 20% greater for the bridge-run machine. At speeds near rated conditions, however, the torque outputs of the two machines are nearly the same.
Fig. 2. Average torque of capacitor run and capacitor bridge run machines — Bridge phase adjusted for maximum torque.

Fig. 3. Pulsating torque of capacitor run and capacitor bridge run machines — Bridge phase adjusted for minimum torque.

Pulsating Torque

Fig. 3 shows the pulsating torque of the capacitor bridge-run machine and 5-μF capacitor-run machine for all load torques from zero to twice the 2.0-Nm rated load. The capacitor bridge machine operation was simulated with the bridge phase adjusted at each load torque to minimize the torque pulsations. For loads less than 2.0 Nm, the capacitor bridge machine has significantly lower torque pulsations. For larger loads, however, the two curves are similar.

THE EFFECT OF CHANGES IN SYSTEM PARAMETERS

The system of the previous section had a properly adjusted bridge phase for “optimal” operation, a large capacitor of 100 μF to avoid any complications produced by ripple in the dc voltage and a fixed auxiliary to main winding turn ratio of 3.4:1. To illustrate the range of options and tradeoffs inherent in the capacitor bridge machine, a number of variations from this nominal system are now considered.

Bridge Phase

The adjustment of the capacitor bridge voltage phase angle is the fundamental control for system operation. The effects of adjustments in the phase relationship between $V_{ref}$ and the source voltage on machine operation are considered for one run and one start condition. The capacitor voltage is kept constant to eliminate any transients.

Run Conditions: Fig. 4 shows phasor diagrams of the currents and fundamental voltages from an analog simulation of machine operation with the rated load of 2.0 Nm for three different bridge phase angles. Diagram 1 shows the machine voltages and currents with an arbitrarily large bridge phase of 90°. The bridge voltage for this case is large, and a large auxiliary voltage and auxiliary current results. The main and auxiliary winding currents are far out of quadrature and the machine is poorly balanced.

At the other extreme, Diagram 3 of Fig. 4 shows simulated machine voltages and currents with an arbitrarily small bridge phase of 60°. In this case, the bridge voltage magnitude is small, and the auxiliary voltage and current are also small. Although the two currents are nearly in quadrature, the main winding current is much larger than the auxiliary current, and the machine is not well balanced.

The conditions of Diagrams 1 and 3 are the extremes, and the “optimal” condition is shown in Diagram 2. The bridge voltage phase angle is 75°, and the two voltages along with the two currents are nearly balanced. The auxiliary voltage is close to 3.4 (equal to the main auxiliary to main winding turn ratio) times the size of the main winding voltage, and the two voltages are close to being in quadrature. The currents are related in the same manner. This bridge phase angle was found experimentally to give the most balanced machine operation.
Fig. 5. Pulsating torque of capacitor bridge run machine for bridge phase angles of (a) 90°, (b) 75°, and (c) 60°.

Fig. 6. Phasor diagrams for capacitor bridge run machine at 10% speed for bridge phase angles of 83° and 66°.

The machine torque waveforms for the three conditions of Fig. 4 are shown in Fig. 5. An unbalanced motor has a double frequency torque pulsation, and it can be seen that of the three conditions shown, the bridge phase of 75° gave much lower torque pulsations. The machine slip was significantly different for the three conditions of Fig. 4. The machine run with bridge phases of 90, 75, and 60° had slips of 0.05, 0.03, and 0.05, respectively.

Start Condition: Two phasor diagrams are shown for the motor simulated under the start condition of 10% speed in Fig. 6. Diagrams 1 and 2 show the motor with arbitrarily large and small bridge phases of 83° and 66°. The magnitudes of the voltages and currents are nearly the same for both cases. The main and auxiliary winding currents are closer to being in quadrature for the condition of Diagram 2, and the machine runs more balanced with a slightly greater average torque output. However, the effect of this large change in the bridge phase on the machine currents at start up is much less than for the run condition previously described. This suggests that the effect of the bridge phase on effective capacitance and machine performance at start up is much less than for the run condition.

Effective Capacitance

The results above illustrate that the capacitor bridge circuit acts as a capacitive element in the complete motor system. The phasor diagrams of Figs. 4 and 6 show that the current into the bridge circuit \( I_{aux} \) always leads the bridge output voltage \( V_{br} \) by 90°. The effective capacitance at the output of the bridge circuit can be calculated from

\[
C_{eff} = \frac{|I_{aux}|}{(\omega |V_{br}|)}.
\]

The value of this effective capacitance changes when the bridge phase is adjusted for any machine operating condition. To show the relationship between the bridge phase and effective capacitance, plots of effective capacitance versus the bridge voltage phase angle for simulated machine operation are shown in Fig. 7. Plots are shown for both motor operation with rated load and for a starting case at 10% speed.

Both plots show that the effective capacitance increases with increases in the bridge phase. However, the effective capacitance was always much larger for the start condition than for the run condition. The plots for all run conditions are nearly identical to that shown for rated load.

DC Capacitor Size

The results shown to this point were simulated for operation with a large dc capacitor of 100 \( \mu \)F to eliminate any significant voltage ripple. In practice, it is desirable to use the smallest possible capacitor. As the capacitor size is reduced, a voltage ripple at twice the supply frequency is superimposed on the dc voltage. This causes the auxiliary current and torque pulsations to become nonsinusoidal. Fig. 8 shows the capacitor voltage, auxiliary current, and torque for the machine run at rated load and starting at 10% speed with a dc capacitor size of 5 \( \mu \)F. The capacitor voltage ripple is much larger for the starting condition than the run condition. However, the distortion of the auxiliary current and torque waveforms is much greater for the run than the start condition.
Auxiliary Current

Torque

(b)

Fig. 8. Effect of dc ripple on waveforms: (a) 10% speed, dc capacitance = 5 pF, bridge phase = 66°; (b) rated torque, dc capacitance = 5 pF, bridge phase = 75°.

Modulation Scale Factor

Adjustments in the modulation scale factor “a” were confirmed by simulation to have no effect on machine operation. However, they do have important effects on the capacitor bridge operation and the sizing of its components. It is possible to show these effects analytically.

Based on the switching algorithm and the requirement that the instantaneous power flow at the bridge output must equal the power delivered to the capacitor, the relationships showing the effects of “a” are

\[ V_{br} = aV_{cap} \]  \hspace{1cm} (1)

\[ I_{cap} = (a/2)I_{aux} \]  \hspace{1cm} (2)

where \( V_{br} \) is the peak fundamental bridge output voltage, and \( I_{cap} \) and \( I_{aux} \) are the peak values of sinusoids at twice the source frequency and at source frequency, respectively. If the peak voltage ripple is now constrained, it can be shown that

\[ C_{dc} > a^2C_{eff}/(4k) \]  \hspace{1cm} (3)

where \( C_{dc} \) is the required capacitor value that gives a peak voltage ripple that is less than the fraction \( k \) of the capacitor dc voltage \( V_{cap} \). These equations take only the fundamental components into account and are inaccurate when distortion in the winding currents occurs with large values of \( k \). “a” is the modulation scale factor and may be calculated as

\[ a = V_{ref}/V_r \quad a < 0.9 \]  \hspace{1cm} (4)

where \( V_{ref} \) and \( V_r \) are peak values of the modulation voltages, as is shown in Fig. 1. These relationships show that the value of “a” is critical in determining the dc capacitor requirements.

An equivalent circuit representing the effect of “a” is shown in Fig. 9. This circuit uses a transformer of ratio \( a : 1 \) at the output of a bridge circuit with 100% modulation (\( a = 1 \)). It may be seen that a reduction in “a” increases the capacitor voltage but decreases the capacitor current and required capacitor size.

The transistor-diode switches must have a voltage rating equal to the highest possible capacitor voltage and a current rating equal to the highest possible auxiliary winding current. Lowering the value of “a” increases the required blocking voltage of the switches but does not reduce the current requirements since there is circulating current in the diodes.

In order to eliminate any transient condition that occurs when the capacitor voltage changes, it is advantageous to control “a” to keep the voltage \( V_{cap} \) constant for all conditions. The equivalent circuit of Fig. 9 shows the advantages in minimizing the capacitor requirements by properly adjusting “a” to charge the capacitor to its highest allowable voltage. For these reasons, all calculations for capacitor requirements are made assuming “a” is adjusted for a constant capacitor voltage equal to its maximum allowable value.

Component Requirements and Machine Performance for Different Winding Ratios

In conventional capacitor-run motors, the auxiliary winding has a much larger number of winding turns than the main winding. This large turn ratio allows the capacitor to operate at a higher voltage, thus decreasing its current and size requirement. However, the large winding ratio may be shown to decrease the starting torque and increase the torque pulsations at rated load.

In the capacitor bridge system, the effect of the modulation ratio “a” is equivalent to a variable turn ratio transformer at the bridge output. The value of “a” may be reduced to deliver a high voltage level to the capacitor and reduce its size requirement. For this reason, the conventional criterion for the selection of a winding ratio is no longer valid. This suggests that a lower winding ratio will give better machine performance without a significant increase in component cost.
TABLE II

<table>
<thead>
<tr>
<th>Winding Ratio</th>
<th>&quot;a&quot; for V_{cap} = 600v</th>
<th>V_{br} (peak)</th>
<th>I_{cap} (rms)</th>
<th>I_{sw} (peak)</th>
<th>I_{max} (rms)</th>
<th>Capacitor Size for 20% rip.</th>
<th>Capacitor Size for 10% rip.</th>
<th>C_{eff}</th>
<th>Average</th>
<th>Load Torque = 2.0 Nm</th>
<th>Pulsating Torque</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.0: 1</td>
<td>.36</td>
<td>218 V</td>
<td>.76 A</td>
<td>5.92 A</td>
<td>4.20 A</td>
<td>11.7 \mu F</td>
<td>11.9 \mu F</td>
<td>13.7 \mu F</td>
<td>0.66 Nm</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2.8: 1</td>
<td>.36</td>
<td>218 V</td>
<td>.39 A</td>
<td>3.02 A</td>
<td>2.14 A</td>
<td>5.96 \mu F</td>
<td>10.5 \mu F</td>
<td>7.3 \mu F</td>
<td>1.44 Nm</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3.4: 1</td>
<td>.36</td>
<td>218 V</td>
<td>.26 A</td>
<td>2.06 A</td>
<td>1.46 A</td>
<td>4.05 \mu F</td>
<td>9.5 \mu F</td>
<td>4.9 \mu F</td>
<td>1.80 Nm</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Illustation of Winding Ratio Changes

The required size of the circuit components is strongly dependent on the winding ratio and desired performance of the system. The required dc capacitance is largely determined by the allowable capacitor voltage ripple. This ripple may be allowed to be larger at startup than during running conditions for the same distortion in machine currents. Ripples of 20% for starting and 10% for running were found experimentally to be tolerable. The transistor switches are required to block the capacitor voltage and conduct the machine auxiliary current.

Table 2 summarizes the simulated machine performance and circuit requirements for both the locked rotor and rated load condition with three winding ratios. The system was simulated in a manner that maximizes the locked rotor torque and minimizes the pulsating torque under run conditions. The capacitor voltage was maintained at 600 V for all cases. To maintain this voltage, the value of "a" is much lower at locked rotor than at full speed. The lower winding ratios are characterized by a larger starting torque and lower torque pulsations at full load. However, the component requirements are greater with the lower winding ratios.

CONCLUSIONS

The capacitor bridge circuit is a workable replacement for standard single-phase induction motor capacitor systems. The new system has been simulated, and results show it to be capable of better performance than an ac capacitor-run motor. The simulations also showed the following:

- The bridge voltage phase angle is the most important adjustment in the system and gives direct control of the bridge circuit effective capacitance.
- The effects of the modulation scale factor "a" are equivalent to the effects of a variable-turn ratio transformer at the bridge circuit output.
- There are further advantages in system operation that are made possible by changing the machine auxiliary to the main winding turn ratio or other design parameters.

REFERENCES


Terrance A. Lettenmaier received the B.S.E.E. degree from the University of Washington, Seattle, in 1983 and the M.S.E.E. degree from the University of Wisconsin, Madison, in 1986. He is presently an engineer at Avtech Corp., Seattle, WA. His professional interests are in power electronics and controls.

Donald W. Novotny (F’87) received the B.S. and M.S. degrees in electrical engineering from the Illinois Institute of Technology, Chicago, in 1956 and 1957, respectively, and the Ph.D. degree from the University of Wisconsin, Madison, in 1961. Since 1961, he has been a member of the faculty at the University of Wisconsin, Madison, where he is currently Professor and co-director of the Wisconsin Electric machines and Power Electronics Consortium (WEMPEC). He served as Chairman of the Electrical and Computer Engineering Department from 1976 to 1980 and as an Associate Director of the University-Industry Research Program from 1972 to 1974 and from 1980 to the present. He has been active as a consultant to many organizations and a Visiting Professor at Montana State University, the Technical University of Eindhoven, Netherlands, the Catholic University of Leuven, Belgium, and a Fulbright Lecturer at the University of Ghent, Belgium. His teaching and research interests include electric machines, variable-frequency drive systems, and power electronic control of industrial systems. Dr. Novotny is a member of ASEE, Sigma Xi, Eta Kappa Nu, and Tau Beta Pi and is a Registered Professional Engineer in Wisconsin.

Thomas A. Lipo (M’64–SM’71–F’87) is a native of Milwaukee, WI. He received the B.E.E. and M.S.E.E. degrees from Marquette University, Milwaukee, WI, in 1962 and 1964 and the Ph.D. degree in electrical engineering from the University of Wisconsin in 1968. From 1969 to 1979, he was an electrical engineer in the Power Electronics Laboratory of Corporate Research and Development of the General Electric Company, Schenectady, NY. He became Professor of Electrical Engineering at Purdue University in 1979, and in 1981, he joined the University of Wisconsin in the same capacity. He has maintained a deep research interest in power electronics and ac drives for over 25 years. In addition to ten patents, Dr. Lipo has received 12 IEEE prize paper awards for his work, and he was co-recipient of the Best Paper Award for the IEEE Industry Applications Society Transactions for the year 1984. In 1986, he received the Outstanding Achievement Award from the IEEE Industry Applications Society for his contributions to the field of ac drives, and in 1990, he received the William E. Newell Award of the IEEE Power Electronics Society for his contributions to power electronics.