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## The Predictive Power of the Yield Curve across Countries and Time

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# The Predictive Power of the Yield Curve across Countries and Time

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**Abstract:** In recent years, there has been renewed interest in the yield curve (or alternatively, the term premium) as a predictor of future economic activity. In this paper, we re-examine the evidence for this predictor, both for the United States, as well as European countries. We believe a re-examination is warranted, both because of the phenomenon of the "conundrum" in the mid-2000's, and the advent of the euro in 1999. We examine the sensitivity of the results to the selection of countries, and time periods. We find that the predictive power of the yield curve has deteriorated in recent years. However there is reason to believe that European country models perform better than non-European countries when using more recent data.

**Key words:** yield curve, term premium, expectations hypothesis of the term premium, industrial production, recession

JEL classification: C22, E37, E43

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#### 1. Introduction

Over two years ago, several observers noted the inversion of the yield curve in the United States. That event sparked a resurgence in the debate over the usefulness of the yield curve as an indicator of future economic activity, with an inversion indicating a slowdown (and in some formulations, a recession). The inverted yield curve as recession indicator, while common in the United States, is not widely used in other countries. Moreover, in the most recent episode, there was widespread conviction that — in light of the increased credibility ascribed to monetary policy — the yield curve no longer served as a useful early warning signal for growth slowdowns. Figure 1 displays the yield spread, the difference between long and short term government interest rates, through time for the United States and select European countries. The yield spread dips before each recession period and turns negative for all but one, including the recession beginning in 2007. For European countries, the relationship is not as consistent but there does appear to be some level of coincidence.

The motivation for studying the yield spread is of course manifold. First, policy makers often need to make decisions today, based on expectations regarding future economic conditions. Although policymakers rely on a range of data and methods in forecasting future conditions, movements in the yield curve have in the past proved useful, and could still represent a useful additional tool.

Second, variations in the correlations between asset prices and economic activity might inform debates regarding the workings of the macroeconomy. The fact that it

works for some countries, and not others, might be suggestive of certain channels being important, to the exclusion of others. A similar sort of reasoning applies to examining the goodness of fit over different time periods.

While there is already a voluminous literature on the subject of yield curves and US economic activity, we nonetheless believe now is an opportune time to re-examine the evidence. This conviction is rooted in two developments.

The first is the advent of the euro in 1999. The creation of a more integrated European bond market, and increased economic linkages on the real side, suggests that the old historical links (or nonlinks, as the case may be) between the interest rates and output might have changed. Yet, until recently, there had not been a sustained and significant downturn in the European economy post-EMU, and hence little opportunity to test the predictive power of the yield curve in this context.

The second is the "conundrum", i.e., the failure of long-term interest rates to rise along with the short-term policy rate, as the Fed Funds rate rose during 2004-05. Some people ascribed this phenomenon to the disappearance of risk, variously associated with the cross-country decline in inflation and output volatility – what is sometimes called the Great Moderation – or with greater risk-management on the part of financial institutions. Alternatively, attention has been directed to the demand by pension funds

for long-term assets, or foreign central bank purchases of Treasury assets.<sup>1</sup> Regardless of the merit of such arguments, we think it of interest to determine whether the previously extant correlations hold in the more recent period.

The paper is organized in the following fashion. In section 2, we lay out a framework for examining what determines the long term interest rate relative to the short, and relate that to the extant literature on the yield curve as a predictor of future economic activity. In section 3, we describe the data and the empirical tests we implement. In Section 4, we repeat the exercise, but using as a dependent variable a binary dependent variable called "recession". Section 5 concludes.

#### 2. Background

#### 2.1 Theoretical Framework

Following previous literature, this paper focuses on the yield spread defined as the 10-year government bond yield less the 3 month treasury yield (or closest equivalent for countries other than the United States)<sup>2</sup>.

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<sup>&</sup>lt;sup>1</sup> See for instance Warnock and Warnock (2006). A contrasting view is in Rudebusch et al. (2006) and Wu (2008).

<sup>&</sup>lt;sup>2</sup> Using aggregate Euro area data, Moneta (2003) found that the 10-year/3-month spread specification performed better than any other pair of yield maturities that included two of the following: 3-month, 1-year, 2-year, 5-year, 10-year.

The linkage between the long-term and short-term interest rates can be decomposed thus:

$$i_t^n = \frac{(i_t + i_{t=1}^e + \dots + i_{t+n-1}^e)}{n} = l_t^n$$
(1)

Where  $i_t^n$  is the interest rate on a bond of maturity n at time t, is the expected interest rate on a one period bond for period t+j, based on information available at time t, and  $l_t^n$  is the liquidity (or term) premium for the n-period bond at time t. This specification nests the expectations hypothesis of the term structure (EHTS) (corresponding to the first term on the right hand side of equation 1), and the liquidity premium theory (corresponding to the second term).

The EHTS merely posits that the yield on a long-term bond is the average of the one period interest rates expected over the lifetime of the long bond. The liquidity premium theory allows that there will be supply and demand conditions that pertain specifically to bonds of that maturity. The presence of idiosyncratic effects associated with a certain maturity of bond is sometimes linked to the "preferred habitat theory", the idea that certain investors have a preference for purchasing assets of specific maturities. Since  $l_t^n > 0$  and is expected to rise as n becomes large, the yield curve will slope upward when short rates are expected to be constant over time.

Now, for the sake of simplicity, consider the case where  $l_t^n=0$  (i.e., the EHTS explains all variation in long rates). Suppose further expected short rates are lower than

the short rate today. Then the long rate will be lower than the short rate (i.e., the yield curve inverts). Since low interest rates are typically associated with decreased economic activity, an inverted yield curve should imply an expected downturn, especially given that  $l_i^n > 0$ , then an inversion should imply a downturn a fortiori.

Why should short interest rates be lower during an economic downturn? The reasoning follows two – not necessarily mutually exclusive -- avenues. The first is that decreased economic activity decreases private sector demand for credit; at the same time the monetary authority is likely to have decreased the policy rate in response to the slowdown. The second is that the monetary authorities raise rates that precipitate the subsequent slowdown.

#### 2.2. Selective Literature Review

The literature on the usefulness of the yield spread in forecasting future growth is extensive and we review only a subset of the analyses here. Some early studies regarding the relationship between growth and the yield spread date to the late 1980s; Harvey (1988, 1989), Stock and Watson (1989), Nai-Fu Chen (1991), Estrella and Hardouvelis (1991) among others, suggested that an inverted yield curve (in this case a negative yield spread) could signal an impending recession. These early studies were primarily conducted using U.S. financial data to predict future Gross Domestic Product (GDP) growth.

Some subsequent research focused on whether the relationship between the yield spread and future economic growth held up in countries other than the United States. Harvey (1991), Davis and Henry (1994), Plosser and Rouwenhorst (1994), Bonser-Neal and Morley (1997), Kozicki (1997), Estrella and Mishkin (1997) and Estrella, Rodrigues and Schich (2003) studied non-US OECD countries using post-1970 data, and generally conclude that the yield spread can be used to some extent in predicting future economic growth. However out-of-sample studies conducted by Davis and Fagan (1997) and Smets and Tsatsaronis (1997) using, respectively, U.S. and German data, and European data, found that parameter estimates are unstable over time. Moreover, the estimated regressions exhibited poor forecasting capabilities.

While the most simple model requires only a single-variable specification with the yield spread as the lone independent variable, some subsequent research allows for additional variables, such as the short term policy rate -- at least when predicting recessions (as opposed to growth). One prominent example of this approach is Wright (2006). In his paper, Wright argues that adding the short-term rate strengthens the insample forecasting results when using a probit model to predict recessions.

#### 3. Empirical Model and Results

#### 3.1 Data

The compilation of the dataset confronts the researcher with many choices, including the set of countries to study, and the choice of both regressors and regressand. We opted to select countries in order to adequately represent the Euro Area. Countries outside the Euro Area provide a basis of comparison to provide perspective and sense of robustness regarding the results.

In addition, to ensure the interest rates represent market-determined rates, we selected countries that have robust and liquid financial markets. The need for a sufficiently large time sample (1970- September 2009<sup>3</sup>) further restricted the set of countries we could examine. Given these constraints, we restrict our analysis to Canada, France, Germany, Italy, Japan, the Netherlands, Sweden, the United Kingdom, the United States. In addition, we estimate an aggregate Euro Area specification using data from 1990-2009. (For tables 4-7, the data extend only to 2008.)

We select industrial production as our measure of economic activity. While GDP is the broadest indicator of economic activity, the use of industrial production presents some substantial advantages in terms of timeliness and reliability.<sup>4</sup> In any case, growth rates of industrial production tend to follow GDP closely<sup>5</sup>. All of the countries in the data set (including the Euro Area) report industrial production at a monthly frequency

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<sup>&</sup>lt;sup>3</sup> For Italy and the Netherlands, the data begin in 1971 and 1972 respectively.

<sup>&</sup>lt;sup>4</sup> By reliability, we mean that the industrial production series do not get revised as significantly as GDP.

<sup>&</sup>lt;sup>5</sup> For instance, the correlation between GDP and IP growth in the US and UK are .76 and .72 respectively.

while GDP is reported at a quarterly frequency; using IP therefore affords us a larger data set.

In terms of our recession indicators, we use the NBER measure for the United States. Since there are not comparable measures for the other countries, we use the recession indicator from the Economic Cycle Research Institute (ECRI).

#### 3.2 In-sample Results

We start with a simple bivariate model:

$$IPGrowth_{t,t+k} = \beta_0 + \beta_1 Spread_t + \varepsilon_{t+k}$$
 (2)

Where  $\mathit{IPGrowth}_{t,t+k}$  is the annualized growth rate over the period t through t+k, and  $\mathit{Spread}_t \equiv i_t^{10\,yr} - t_t^{3mo}$ .

In words, the yield spread at time t predicts the annual growth rate of industrial production from time t to time period t+k months. We examine this model with k equal to 12 and 24 (i.e. growth over a one and two year time horizon). Since adjacent year over year growth figures will be drawing from overlapping data points, the resulting error terms will be serially correlated. To account for this serial correlation, we

conduct our statistical inferences using heteroscedasticity and serial correlation robust standard errors. <sup>6</sup>

We turn first to the results from the model using the complete data set (1970-2008), displayed in table 1. All countries exhibit a significant slope parameter over the one year forecast horizon (at the 5 percent significance level for all but the Euro Area where it is significant at the 10 percent level), suggesting the yield spread may hold some forecasting value. The magnitude of the parameter estimate is also economically significant. Take the slope coefficient of 1.38 for France, for example; this point estimate implies that for each percentage point increase in the yield spread, French industrial production growth will increase by 1.38 percentage points.

Figure 2 displays the estimated slope coefficients for all countries in the data set.

These coefficients vary markedly across countries, ranging from a high of 1.85 in Canada to a low of 0.75 in the Sweden. A chow test confirms the fact that the relationship between the yield spread and economic growth is not identical across countries.

Despite the existence of statistically significant parameter estimates in each country, the goodness of fit for the model (according to the R-squared statistic), varies substantially across country models. That being said, the *relative* proportion of variation across countries is of interest. The yield spread in United States, Germany, France and

<sup>&</sup>lt;sup>6</sup> We have investigated whether the variables are stationary or not. Unit root tests indicate that the spreads and industrial production changes are stationary.

Canada explains more than 20 percent of the changes in annual industrial production growth. In contrast, the yield spread explains less than 10% of the variation in output in Italy, the Netherlands, and Sweden.

Following Bonser-Neal and Morley (1997) and Kozicki (1997), we also examine the corresponding specification for growth over a two year horizon. While many of the variables are still significant, the explanatory power of the model deteriorates for many countries. Additionally, in every case the magnitude slope coefficient is smaller in the two-year model relative to the one-year model. The decrease in explanatory power and magnitude of the coefficient estimates at the two-year versus one-year horizon suggests most of the explanatory power is concentrated at the former horizon. Figure 3 displays the goodness of fit according to the R-squared coefficient across countries over one and two-year growth forecast horizons. Only the German, United Kingdom and United States models exhibit better fit in the two-year model relative to the one-year model.

In order to investigate the time variation in the strength and nature of the yield curve/growth relation, we split the sample at 1997/98. The choice of that specific date is primarily pragmatic in nature; it sets each subsample to be roughly similar in size. At the same time, the choice is somewhat fortuitous, as the latter subsample then conforms approximately to the post-EMU period.

<sup>&</sup>lt;sup>7</sup> For an empirical investigation into this issue see Kozicki (1997).

Tables 2 and 3 contain results from the two sub-samples of data, and highlight a key finding. The detection of a statistically significant relationship between term spreads and subsequent output growth is driven by the early portion of the sample. The regressions on date from the early sample (1970-1997) yield coefficients that are significant for every country at the 95 percent confidence level. In contrast, the coefficient estimates when using more recent data (1998-2008) are significantly different from zero in only four of nine countries, suggesting a general deterioration in the relationship between the yield spread and economic growth in recent years.<sup>8</sup>

Examining the goodness of fit across sub-samples in figure 4 leads to similar conclusions. Only the Sweden and Italy models exhibit a better fit when using the later data subset. In Italy's case the slop coefficient is not significant at the 95 percent confidence level. Only in four (very important) cases – the US, France, Germany and Italy — does the the goodness of fit hold steady. Japan exhibits the sharpest dropoff in goodness of fit from the two subsets, starting at nearly 0.2 in the 1970-1997 subsample and reaching nearly zero in the 1998-2008 subsample. This data period coincides with the Asian financial crisis and may reflect Japan's short term rates hitting the zero interest lower bound.

One interpretation of the negative coefficient could be as follows: typically a central bank will lower the policy rate to stimulate the economy. To the extent that the

<sup>&</sup>lt;sup>8</sup> Interestingly the level of the coefficient for Sweden is three-fold higher in the later sample relative to the early sample.

long-term rate is less responsive to policy rates compared to short-term rates a lowering of the policy rate correlates with an increase in the yield spread. When the policy rate hits zero and the central bank engages in quantitative easing to replace reductions in the policy rate, longer term interest rates fall. The result is a narrowing of the yield spread. If successful, these lower long-term rates should spur the economy and future growth should be on the horizon. If this were the case, and if the only shocks hitting the economy were varations in the extent of quantitative easing, we would expect the relationship between the yield spread and future growth when the policy rate is at zero to be inverse to the reationship when the policy rate is positive. One implication of the Japanese results, relevant to current debates is that going forward, is that we might expect a degraded fit for the US yield curve/output relationship, given the effective Fed Funds rate has essentially hit zero.

Haubrich and Dombrosky (1996) and Dotsey (1998) suggest that the relationship between the yield spread and future growth diminishes using data since 1985. The results of our analysis suggest that the relationship continues to deteriorate post 1997, but with a couple of exceptions.

#### 3.3 Out-of-Sample results

A common critique of in-sample estimation is that the model estimates the fitted values using data that would not have been available at the time of the observation being fitted. The results of an in-sample forecast will be using extra information to fit the parameters to the data and could therefore overstate the

predictive power of the independent variable. If we were to attempt to forecast growth from today to one year into the future, we would not be privy to the information in the interim.

One way to circumvent this potential problem is by conducting a pseudo out-of-sample regression analysis. Each yield spread observation is used to predict future growth with truncated data such that the only data used is data that existed prior to the observation. For example, if we have a data set that ranges from 1970-2008 and we want to predict industrial production growth from January 1980 to January 1981, we could restrict our regression to only use data from 1970-1979 in calculating the constant and slope parameters for our estimation of 1980-1981 growth. Then, to estimate IP growth from February 1980 to February 1981, we re-run the regressions adding the January 1980 data and use the newly generated parameter estimates to predict growth over that time period.

The parameter estimates from the recursive regressions are used to generate a series of fitted values for year-over-year growth for each country. We opt to compare the root mean square error (RMSE) criterion, and compare against a naïve forecast RMSE. In this case, our naïve forecast is a simple AR1 model of growth.

The results can be succinctly summarized. We conclude that there exists a marginal benefit to estimating a growth model with the yield spread (as opposed to the simple AR(1) model) if the RMSE from the yield spread model specification is less than that of the AR(1) model. Figure 5 displays the fitted values for the out-of-sample model,

using the yield spread as the independent variable. While extreme fluctuations were not always well predicted, the general shape of the data seems to be captured in many cases. None of the models, including those that outperformed the AR1 models, were able to predict the most recent contraction of industrial production.

Results relative to the AR(1) model across all countries were mixed. Table 4 displays the results of the RMSE scores for both model specifications. Four of the nine country models scored lower RSME from the yield curve specification as opposed to the AR(1) model, while the remaining five increased. All four of the yield curve models exhibiting lower RMSE than the AR(1) models were European countries.

The relatively poor out-of sample results could, in part, be due to fundamental changes in the relationship between the yield curve and economic activity over time. If the structure of the relationship changed in the middle of our sample the forecasting power, coefficient estimates using historical data may not be useful in predicting growth out of sample. A number of events over the past ten years may have affected the predictive power of the yield curve including: the advent of the European monetary union, the "great moderation", the global savings glut and the Japanese experience with a zero lower bound policy rate. Each of these events affected different subsets of countries within our dataset therefore if we witness a simultaneous deterioration of predictive power across countries affected by the same event, it may suggest that that event was partially responsible for the observed deterioration. For instance, if each model corresponding to a country that adopted the Euro exhibits a simultaneous drop in

the significance of the yield curve coefficient shortly after the advent of the euro (and relative to other countries), this may suggest the adoption of the Euro changed what the yield curve tells us about future economic growth.

To examine changes in the predictive power of the yield curve through time we use rolling window regressions. The dataset for the first regression for each country is restricted to include only data from January of 1970 through December of 1979. The dataset for the next regression is restricted to data from February of 1970 through January of 1980, and so on. Figure 6 plots the coefficient estimate and 95% confidence intervals corresponding to the yield curve for each overlapping 10 year interval from January 1970 – December 1979 through January 1999 –December 2008. The grey shaded area roughly approximates the time period of interest including the global savings glut, European monetary union and the second half of the "great moderation". Generally declining coefficient estimates and widening confidence bands confirm our suspicion that the relationship between the yield curve and economic growth has deteriorated over the last ten to fifteen years. However many models exhibit a strengthening over the past one or two years.

The Euro area countries appear similar to one another in some respects: the coefficient estimates tend to decline into 1990 when they generally become insignificant. This is consistent with the fact that many macroeconomic variables (including both industrial production and the yield spread) became significantly less volatile decreasing the detectibly of any relationship. The recent uptick in the

coefficient estimates is consistent with recent macroeconomic volatility. However coincidental deterioration is less obvious post 1998 where the coefficient estimates are generally insignificant.

Canada, the United Kingdom and the United States all exhibit deterioration in the post 1998 era; the significance band widens in the United states and Canada while the coefficient estimate draws closer to zero in the United Kingdom. Some have speculated that the global savings glut may have affected not only the United States but also other countries with strong legal regimes and liquid financial markets<sup>9</sup>. If Canada and the United Kingdom were affected by the global savings glut in the same way that the United States may have been, this is the coincidental deterioration one might expect. Certainly there exist other potential confounding factors, yet it remains and interesting coincidence.

Finally, Japan may have been the most dramatic of all models in our sample. As the regression begins to include data after the zero lower bound policy rate the coefficient estimate swings wildly to the negative side (albeit mostly insignificant). However the estimate swinging negative is what we would have expected as the short rate hits zero and the government attempts to lower long-term rates as well.

#### 3.4 Real-time data results

<sup>&</sup>lt;sup>9</sup> See, for example, the 2009 Economic Report of the President, Chapter 2.

In the previous exercises we used historical data as they looked at the time. However industrial production data, as are most measures of economic activity, is subject to revision. For instance, United States industrial production for December 2008 was originally reported as 106.1 by April 2009, December data had been revised down to 104.8. From a forecasting perspective, using data as it appears most recently (the current vintage) is not the same as using data as it looked prior to the estimation period. If, today, we want to evaluate how the model would have performed in December 2008, using data as it appeared in December 2008 as opposed to today, more closely simulates estimating the model in 2008.

Koenig, Dolmas & Piger (2003) point out that the relationship between early estimates of economic output and early estimates of explanatory variables is the relationship of interest to forecasters. Any given vintage prior to a forecasting period will have historical figures that have been revised as well as early estimates of more recent data. To capture the relationship between early estimates of output and explainatory variable Koenig, Dolmas & Piger suggest creating a "real-time vintage" by compiling a single time series for each variable that include only the first estimate. Furthermore, Koenig, Dolmas & Piger argue that revisions to data are unpredictable (essentially extraneous noise) at the time if issuance so using a real-time vintage on the left-hand side of an equation eliminates the noise and in fact provides more accurate forecasts.

In this section we use real-time vintage data created from the OECD Main Economic Indicators real-time data and revisions database<sup>10</sup>. Due to data availability, we use GDP deflated by CPI as a measure of economic output and restrict our sample of countries to: Canada, Germany, Japan, U.K. and U.S. Since the interest rates used to construct the yield spread are not typically revised, therefore using the current vintage for the yield spread sufficiently represents a real-time vintage. Each data point in the GDP growth real-time vintage represents the first estimate of nominal four-quarter growth deflated by CPI.

Table 5 displays the results of the real-time data estimation. For comparison, the second column displays estimates of the same equation using a single, recent vintage. Significant parameter estimates across all countries, except Japan, suggest the yield curve does tend to provide significant information regarding first estimate economic growth over the next four quarters. However, the real-time data does not appear to significantly outperform single-vintage data when using the full sample of data.

We next turn to out of sample estimation with the real-time vintage data to test forecasting performance. The RMSE of the recursive estimates are displayed in table 6. The results from the real-time vintage data are compared with results from the current vintage. In all cases excluding Germany, the real-time data provided more increased forecasting power. If revisions are indeed unpredictable at the time of the initial

<sup>&</sup>lt;sup>10</sup> Vintages prior to 2004 were graciously provided by Lucio Sarno, as used in Sarno and Valente (2009)

estimate, stripping the added noise caused by the revisions could be driving the improved performance of the real-time equation.

#### 4. The Yield Curve and "Recessions"

We now move to a nonlinear version of the same question we asked earlier, to the extent that recessions are a specific characterization of (negative) output growth. Following Montea (2003) and Wright (2006), we test if the yield spread is a predictor of recessions, defined as a binary dependent variable.

Clearly there is little agreement in terms of the findings in the literature, especially in this cross-country context. While Montea (2003) finds the yield curve alone is a useful predictor of recessions when using aggregate Euro area data, Wright (2006) argues there is no reason to believe that an increase in the short-term interest rate should have the same consequence as a decrease in the long term rate. Consequently, augments the conventional recession/yield curve specification with the Federal funds rate to isolate the effect of changes in the short-term rate. Indeed, Wright's model performed better when adding the federal funds when using United States data. Following the literature, the models we use are as follows:

$$Pr(R_{t+1,t+k} = 1) = \phi(\beta_0 + \beta_1 Spread_t)$$

$$Pr(R_{t+1,t+k} = 1) = \phi(\beta_0 + \beta_1 Spread_t + \beta_2 3mo_t)$$

Where t is the current time period and k is the forecast period and  $\phi(\cdots)$  denotes the standard normal cumulative distribution function. We use the 3-month interest rate to isolate the effect of movements in short-term interest rates. The recession indicator equals one if there is a recession in any month between t+1 through t+k, inclusive We estimate both models using k equal to 6 and again with k equal to 12 (i.e. a six month and one year forecast).

Table 7 displays the results from the probit model estimates for each country. The first two columns are the results from a six-month forecasting horizon, while the third and fourth columns display the twelve-month forecasting results. The pseudo R-squared statistic (which does not penalize for increased model size) is shown as an indicator of goodness of fit. Generally the models that include the short-term interest rate out-perform those that only include the yield spread.

For the United States, our results differ somewhat from the results obtained by Wright (2006); the yield spread parameter is significant over both the six-month and twelve-month forecasting periods. However, the 3-month interest rate parameter is statistically insignificant over either horizon. Additionally, we do not see a significant increase in goodness of fit when adding the short-term rate.

The results from the Germany model are very similar to the United States model: model performance improves very little when adding the short-term interest rate and the short-term interest rate parameter is not statistically significant. Interestingly, results for the remaining countries outside the United States are starkly different. Across many other non-US countries, adding the short term rate to the model reduces both the magnitude and significance of the yield spread, while increasing the overall goodness of fit. In Canada, Sweden and the United Kingdom the short-term rate is statistically significant while the yield spread coefficient actually becomes statistically insignificant. The most dramatic instance of this is the Canada where the magnitude of the t-statistic for the yield spread parameter declines from negative 5 to just negative 0.5 when adding the short-term rate in the six-month forecast; at the same time the pseudo R-squared statistic jumped from 0.31 to 0.48. In all countries excluding Japan, the coefficient on for the short-term interest rate is positive, suggesting high relative short-term interest rates precede periods of slower growth.

We display in Figure 7 the estimated probabilities of recession in the subsequent 6 months using only the yield spread, and both the yield curve and 3-month interest rate. Generally speaking recessions were well predicted by the yield curve across countries in the 1970s and 1980s. When we look at recessions in the 1990s and 2000s however, results are less consistent. Across most countries recessions earlier in the data set were predicted better when including the short-term interest rate level whereas more recent recessions tend to be better predicted with the yield spread

alone. While this stylized fact may be indicative of a structural change in the relationship between interest rates and future economic activity, it could also be due to the decline in short-term interest rate volatility relative to the decline in yield spread volatility since 1995<sup>12</sup>.

To highlight some specific characteristics of our findings, for Germany estimated probabilities peaked near one hundred percent predicted probability prior to the recessions in the 1970s and 1980s, as anticipated. Additionally the estimated probability exceeded 80 percent preceding the 1990 recession. While the probability peaked at lower levels before the 2000 and 2007 recessions, in both cases the model ascribed a probability well in excess of 50 percent. The results for the United Kingdom and Italy paint a different picture. Probabilities generated by the model fit the recession data well for through 1990; however, models were largely unresponsive in the months leading up to the 2007 recession. In both cases the model excluding the short-term rate actually produced a higher probability of recession then the model including both the yield spread and the short-term interest rate. These performances suggest something may have been structurally different about the recessions of the 2000s. It is tempting to speculate on the impact of Economic and Monetary Union on this phenomenon, since

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<sup>&</sup>lt;sup>12</sup> Variance of 3-month interest rate was, on average, 9.75 times greater in 1970-1994 when compared to 1995-2008 data while the variance of the yield spread was, on average, 4.95 percent higher in 1970-1994 when compared to 1995-2008. Only two countries exhibited increased relative volatility of the 3-month spread: Sweden and Italy.

the 2001 recession is the first one occurring when the ECB was setting short term rates, and long rates had converged to relatively small differentials. 13

Results in Japan are unique across this data set. When using only the yield spread as in independent variable the coefficient is not statistically significant and the model explains almost nothing. When adding the short-term interest rate, both coefficients become highly significant and the explanatory power of the model increases markedly. Additionally, the sign of the short-term interest rate coefficient is negative, suggesting that lower relative short-term interest rates tend to precede times of slower growth in Japan.

#### 5. Conclusion

This paper has explored the importance of the yield spread in forecasting future industrial production growth and recession. Generally speaking, when using the entire data series from 1970-2008, in-sample results suggest the yield spread is indeed important and has significant predictive power when forecasting industrial production growth over a one-year time horizon. The results deteriorate when forecasting growth two years ahead. Moreover, it appears that the predictive power of the yield curve for subsequent one-year growth is much weaker in the last decade. However, four out of six European country models exhibited relatively high R-squared statistics (above 0.1)

<sup>&</sup>lt;sup>13</sup> Note that CEPR, using a methodology reminiscent of NBER's, did not declare a recession for this period. See CEPR at <a href="http://www.cepr.org/data/Dating/info1.asp">http://www.cepr.org/data/Dating/info1.asp</a>.

when using data from 1998-2008, and for two countries (Italy and Sweden) the proportion of variation actually increased. While the explanatory power is somewhat less for certain models estimated over the 1970-1997 data, the data still suggest the yield curve might possess some forecasting power for European countries. The marked deterioration of the significance in the Japan model when using data corresponding to Japan's period of zero interest rate policy (ZIRP) might presage a weakening of the significance of the relationship in the United States, given the effective Federal funds rate has reached the zero lower bound.

The results we obtained in the out-of-sample forecasting exercises were less convincing. Of the European countries examined, only for Germany, Sweden and France did the yield curve possess greater predictive power than a simple AR(1). Certainly the relationship between the yield spread and growth has declined in recent years; however it appears that the relationship has held up best in some European countries and may have strengthened with the increasing volatility of macroeconomic data over the past two years.

The contrast across countries was marked for the probit models. The short-term rate was significant in several instances; however inclusion of the short-rate often resulted in a decrease in the economic and statistical significance of the yield spread. The model predicted recessions relatively well for the US, Germany and Sweden over the entire data set while the remaining models largely failed to anticipate the recessions of the 2000s. The Japanese case is distinct from all the others. Low short-term rates

appear to precede future economic slowdown and the model performs very poorly without the short-term rate.

In other words, we do not obtain a simple story for the yield curve's predictive power. The yield curve clearly possesses some forecasting power. However, there is also some evidence the United States is something of an outlier, in terms of its usefulness for this purpose. And overall, the predictive power of the yield curve seems, with some notable exceptions, to be declining over time.

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#### Data Appendix

Data for this paper came from two sources. All of the recent data came from Haver Analytics. When the series in Haver did not extend back to 1970, the Haver series were spliced with data from the Bonser-Neal and Morely (1997) dataset. These data include the following:

#### Canada:

3-month interest rate from 1/1970 to 12/1979 (IFS) Industrial Production from 1/1970 to 12/1980 (BIS)

#### France:

3-month interest rate from 1/1970 to 5/1989 (BIS) 10-year interest rate from 1/1970 to 8/81 (BIS)

#### Germany:

10-year interest rate from 1/1970 to 12/1979 (OECD, FRB)

#### Italy:

3-month interest rate from 1/1971 to 12/1979 (IFS) 10-year interest rate from 1/70 to 12/79 (BIS, IFS) Industrial Production from 1/60 to 12/79 (BIS)

#### Japan

3-month interest rate from 1/70-4/79 (BIS) 10-year interest rate from 1/70 – 8/87 (BIS)

#### Netherlands

3-month interest rate from 10/72 – 12/81 (BIS) 10-year interest rate from 1/70-4/82 (IFS) Industrial Production from 1/70 – 12/79 (IFS)

#### Sweden

3-month interest rate from 1/70 - 12/82 (IFS) 10-year interest rate from 1/70 - 12/86 (IFS) Industrial Production from 1/70 - 12/89 (FRB)

#### UK

3-month interest rate from 1/1970-12/1985 (FRB)

Where OECD indicates Organization for Economic Cooperation and Development, BIS indicates Bank for International Settlements, IFS indicates IMF, *International Financial Statistics*, and FRB indicates Federal Reserve Board internal database.

Table 1: Yield Curve/Growth Recessions, Full Sample (1970-2009)

	1 Year		2 Year		
	Constant	Slope	Constant	Slope	
Canada Standard	0.208	1.854	0.954	1.212	
Error	0.532	0.209	0.420	0.180	
France	0.271 0.554	<b>1.383</b> 0.338	0.998 0.372	<b>0.527</b> 0.200	
Germany	0.075 0.634	<b>1.416</b> 0.259	0.623 0.372	<b>1.006</b> 0.137	
Italy	<b>1.273</b> 0.629	<b>0.871</b> 0.300	<b>1.567</b> 0.402	-0.025 0.178	
Japan	1.333 0.762	<b>1.299</b> 0.391	<b>1.983</b> 0.553	0.297 0.286	
Netherlands	0.173 0.526	<b>0.946</b> 0.246	<b>0.655</b> 0.244	<b>0.482</b> 0.117	
Sweden	1.021 0.710	<b>0.746</b> 0.263	<b>2.178</b> 0.545	-0.061 0.212	
United					
Kingdom	0.620 0.403	<b>0.882</b> 0.207	<b>0.781</b> 0.285	<b>0.604</b> 0.113	
United States	-0.037 0.628	<b>1.630</b> 0.289	0.362 0.442	<b>1.456</b> 0.190	

Table 2: Yield Curve/Growth Recessions, Early Sample (1970-1997)

	1 Year		2 Year	
	Constant	Slope	Constant	Slope
Canada	0.938	1.991	1.595	1.295
Standard Error	0.604	0.194	0.397	0.172
France	1.110 0.531	<b>1.543</b> 0.355	1.525 0.378	<b>0.633</b> 0.209
Germany	0.485 0.548	<b>1.180</b> 0.214	0.695 0.370	<b>0.920</b> 0.134
Italy	<b>2.624</b> 0.662	<b>1.160</b> 0.335	2.271 0.449	0.177 0.215
Japan	<b>2.547</b> 0.714	<b>1.541</b> 0.390	<b>2.613</b> 0.589	0.491 0.278
Netherlands	0.434 0.535	<b>0.912</b> 0.236	<b>0.770</b> 0.283	<b>0.481</b> 0.121
Sweden	1.792 0.656	<b>0.551</b> 0.234	<b>2.499</b> 0.581	-0.117 0.210
United Kingdom	1.181	0.783	1.273	0.553
O	0.475	0.206	0.333	0.119
United States	-0.030 0.759	<b>2.042</b> 0.352	0.775 0.487	<b>1.515</b> 0.208

Table 3: Yield Curve/Growth Recessions, Late Sample (1998-2009)

	1 Year		2 Year	
	Constant	Slope	Constant	Slope
Canada	-1.138	1.066	-0.812	0.933
Standard Error	1.696	0.705	1.556	0.708
France	-4.091 2.148	<b>2.923</b> 1.237	<b>-2.693</b> 1.334	<b>2.016</b> 0.739
	2.110	1.207	1.551	0.737
Germany	-4.147 1.742	<b>5.055</b> 1.743	-1.855 1.708	<b>3.123</b> 1.055
Italy	<b>-4.955</b> 2.429	<b>3.451</b> 1.462	-1.930 1.750	1.259 0.926
Japan	-8.507 6.627	7.063 4.730	0.925 2.367	-0.447 1.575
Netherlands	-0.846 2.022	1.386 1.335	0.177 0.849	0.625 0.545
Sweden	<b>-7.126</b> 3.262	<b>5.915</b> 2.045	-2.472 2.557	2.678 1.395
United Kingdom	-0.753 0.409	0.808 0.832	<b>-0.730</b> 0.319	0.013 0.454
United States	0.058 0.988	0.316 0.485	-0.611 0.843	<b>1.090</b> 0.311

**Table 4: Out of Sample Forecasting Performance** 

	Yield		
	Spread	AR1	
	RMSE	RMSE	
Canada	4.140393	4.798523	***
France	3.07171	2.915627	
Germany	3.328575	3.785737	***
Italy	4.233276	3.986558	
Japan	5.491521	4.902213	
Netherlands	3.945189	3.889603	
Sweden	4.253046	5.513141	***
UK	2.720546	2.8979	***
US	3.425576	3.388179	

**Notes:** \*\*\* indicates yield spread specification out-performs the AR1 model.

Data sample ranges from January, 1970 to November, 2008.

Table 5: Real-time data

_	Real-Time GDP Vintage		Current Vintage		
	Constant	Slope	Constant	Slope	
Canada	1.569	0.942	2.900	1.088	
Standard	.0441	0.231	0.475	0.232	
Error					
C	0.022	0.701	4 495	0.406	
Germany	0.832	0.701	1.135	0.486	
	0.383	0.160	0.211	0.109	
Japan	1.436	0.057	1.330	-0.191	
)- P	0.447	0.190	0.475	0.164	
United	1.567	0.489	2.522	0.486	
Kingdom	0.310	0.179	0.421	0.210	
migaom	0.510	0.17 5	0.121	0.210	
United States	1.698	0.794	1.850	0.744	
	0.309	0.126	0.326	0.128	

Data sample ranges from 1973Q1 to 2009Q2.

**Table 6: Real Time Out-of -Sample Forecasting Performance** 

	Real-	Current	
	Time	Vintage	
	RSME	RSME	
Canada	2.510	2.604	***
Germany	2.246	2.124	
Japan	2.631	2.720	***
UK	2.393	2.685	***
US	2.029	2.072	***

**Notes:** \*\*\* indicates real-time data out-performs the current vintage data. Data sample ranges from 1973Q1 to 2009Q2.

**Table 7: Probit Model Performance** 

	Next 6 Months		Next 12 Months	
Canada				
Ten-year less Three- Month	-0.526	-0.064	-0.606	-0.140
Three-Month Rate	(0.104)	(0.133) <b>0.317</b>	(0.127)	(0.182) <b>0.345</b>
Pseudo R2	0.307	(0.083) 0.480	0.354	(0.097) 0.533
France				
Ten-year less Three- Month	-0.351	-0.219	-0.402	-0.269
Three-Month Rate	(880.0)	(0.110) 0.100	(0.115)	(0.136) 0.102
Pseudo R2	0.100	(0.058) 0.146	0.117	(0.063) 0.163
Germany				
Ten-year less Three- Month	-0.647	-0.541	-0.602	-0.480
Three-Month Rate	(0.148)	(0.199) 0.083	(0.159)	(0.201)
Pseudo R2	0.324	(0.098) 0.332	0.286	(0.110) 0.299

Italy

-0.111
1) (0.124) 0.052
(0.048)
4 0.087
3 <b>-0.633</b>
3) (0.170) - <b>0.352</b>
(0.091) 0.225
<b>o</b> -0.147
6) (0.154) 0.111
(0.067) 6 0.154
<b>o</b> -0.178
7) (0.152) <b>0.184</b>
(0.079) 0.273
2 -0.573
(0.154) 0.121 (0.110)
2 0.284

Data ranges from January, 1970 to November, 2008.

Figure 1

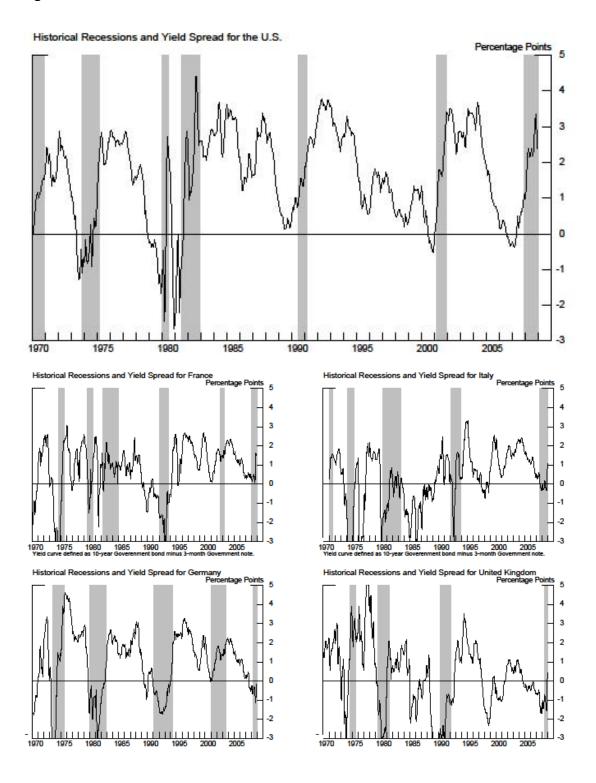
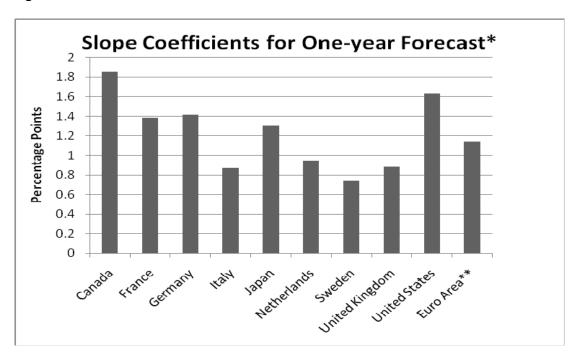


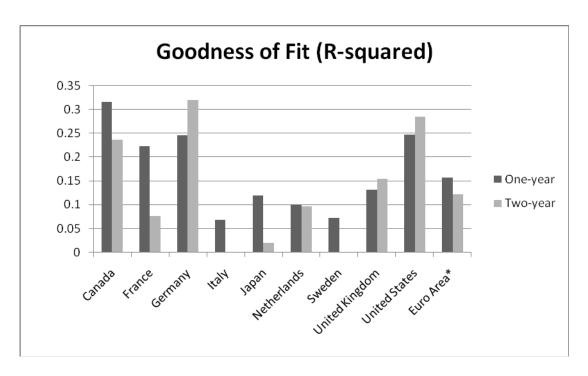
Figure 2



<sup>\*</sup>Effect of a 1 percentage point increase in the yield spread on growth of industrial production

Figure 3

<sup>\*\*</sup>Euro area data from 1990-2008



<sup>\*</sup>Euro area data from 1990-2008

Figure 4

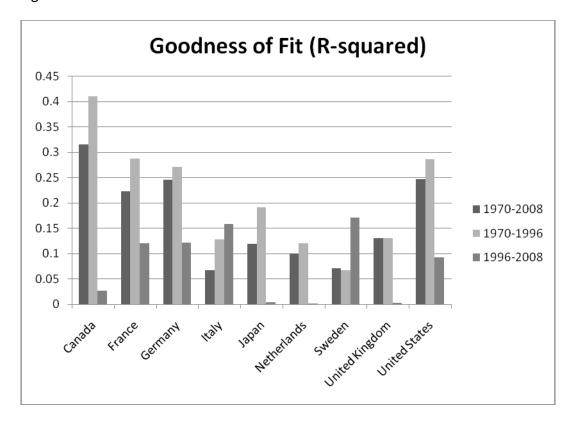


Figure 5

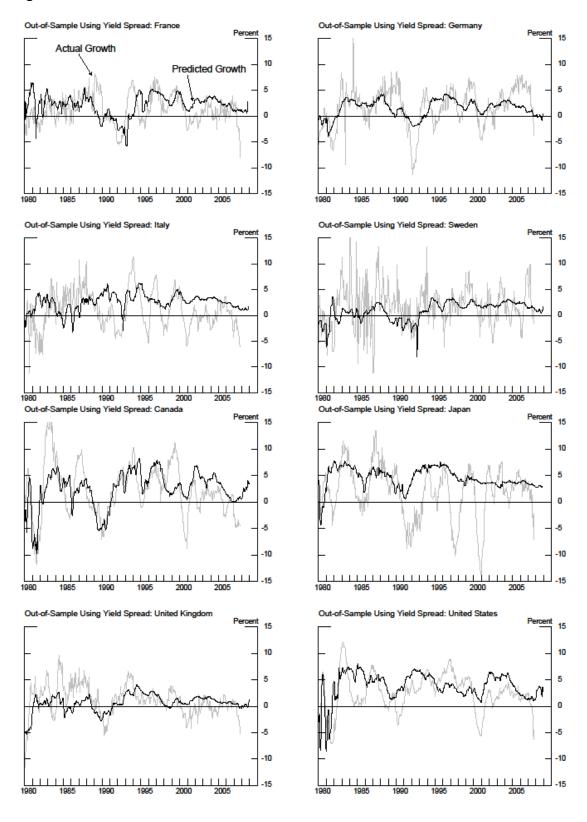
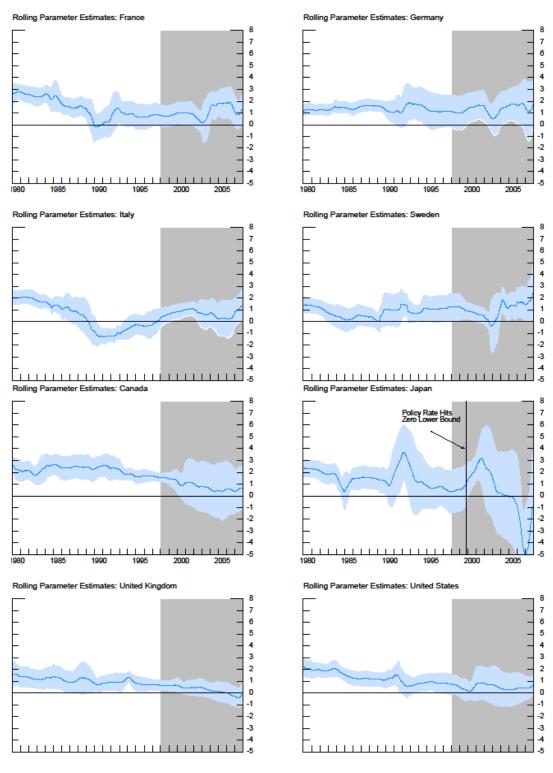


Figure 6



Estimated yield curve coefficient with 95% confidence band.

Figure 7

