AC Brushless Drive With Low-Resolution Hall-Effect Sensors for Surface-Mounted PM Machines

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Abstract—An ac brushless drive in which Hall-effect sensors are used as rotor position sensors is presented in this paper. Three different methods to obtain a high-resolution position estimation from the low-resolution sensors are described and compared through simulation and experimental testing. The proposed control algorithm's most innovative feature is its adaptability to the entire speed range, including startup, when using any of the three estimation algorithms. The control algorithm has been implemented and tested in order to drive a slotless axial-flux permanent-magnet (PM) machine for domestic appliance applications.

Index Terms—Low-resolution sensors, position and velocity estimation, surface-mounted permanent-magnet (PM) machine, vector-tracking observer.

I. INTRODUCTION

AS IT IS well known, position sensors are necessary in brushless drives in order to provide the correct current waveform supply. High-resolution sensors such as optical encoders or electromagnetic resolvers are required for sinusoidal ac brushless drives, in order to guarantee field orientation and low torque ripple. However, these sensors are costly and delicate, and they require special machine construction, such as a second shaft end to couple the sensor. On the other hand, dc brushless drives are fed with 120 electrical degree square-wave currents, which require a 60° resolution in rotor position sensing. In this case, inexpensive Hall-effect sensors are sufficient. As a result, a relatively inexpensive drive can be built, although the tradeoff consists of reduced performances and increased torque ripple.

The position sensorless approach to surface-mounted permanent-magnet (PM) machine control is still an open matter,

and several solutions have been proposed, but none completely solve the problem. Rotor position can be estimated using the back electromotive force (EMF) [1], [2]. These methods generally work well, but fail at very low and zero speeds. Although these machines are nonsalient, high-frequency injection methods can still be used [3]: However, these methods require usage of a consistent portion of the dc-bus voltage and are quite sensitive to different load conditions. To guarantee a full range of operation for a nonsalient machine—including rejecting disturbances at zero speed—position sensors are still required.

Using digital Hall-effect sensors and some additional hardware, a sinusoidal brushless drive has been proposed by Morimoto *et al.* [4]. High-resolution position information is obtained by processing the low-resolution position measurement and by assuming the velocity to be constant throughout a 60° sector, equal to the average velocity in the previous sector. Such an algorithm cannot be used at startup and when accelerating or decelerating at low speeds due to the increased error in position estimation. The authors propose a square-wave startup that allows the drive to start in the correct direction and accelerate until a speed that allows low position estimation error is attained.

Bu *et al.* [5] proposed a software implementation that can substitute the extra hardware introduced in [4] and work correctly even at low speeds. The rotor position estimation error is reset every time the rotor's magnetic axis enters a new 60° sector, since the low-resolution sensors are able to give a correct position value every 60°. This allows proper control at low speeds, although startup is not thoroughly studied.

In [6], an improved position estimation algorithm is presented, adopting a position estimation error compensation taking into account the q -axis reference current. This algorithm can function properly also at startup.

Giulii Capponi *et al.* [7] proposes a dc brushless startup algorithm that allows the drive to start in the correct direction and reach a minimum speed that allows correct position estimation and thus proper ac brushless operation. This minimum speed is proven to be much lower than the one adopted in [4].

In [8], a similar algorithm to the one described in [4] is proposed, but the authors compensate for the load influence on position measurement. The startup algorithm is similar to the one proposed in [7].

In this paper, the control scheme that was proposed in [7] and that is schematically represented in Fig. 1 is

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Fig. 1. Block diagram of the proposed brushless drive.

further studied and improved. Three types of position estimation algorithms are presented and compared. Such a drive can be considered as an intermediate solution between the traditional sensed and the position-sensorless brushless drives. The proposed control algorithm's most innovative feature is its adaptability to the whole speed range, including startup, when using any of the three estimation algorithms. The entire control algorithm has been implemented and tested in order to drive a slotless axial-flux PM machine devoted to domestic appliance applications [11], [12], even though the results are general and can be applied to any surface-mounted PM machine.

II. POSITION ESTIMATION ALGORITHMS

High-resolution rotor position estimation is obtained through digital signal processing of the sensors' outputs.

The sensors detect when the rotor's magnetic axis enters a new 60° sector. The electric angular position is generally expressed as

$$\theta(t) = \int_{t_k}^t \omega(t) dt + \theta_k \quad (1)$$

where $\omega(t)$ is the instantaneous electric angular velocity, t_k is the instant in which the magnetic axis enters sector k ($k = 1, 2, \dots, 6$) and θ_k is the initial angle of sector k , measured from a fixed reference axis.

Three different position estimation algorithms have been studied and compared—two are based on the Taylor series expansion and the third is a vector-tracking observer.

A. Zeroth-Order Algorithm

The zeroth-order position estimation algorithm, introduced in [4], is obtained by taking into account only the zeroth-order term of an approximated Taylor series expansion. This algorithm considers the speed inside each sector to be constant and equal to the average velocity in the previous sector. Rotor speed can then be approximated as

$$\omega(t) \cong \hat{\omega}_{0k} = \frac{\frac{\pi}{3}}{\Delta t_{k-1}} \quad (2)$$

where Δt_{k-1} is the time interval taken by the rotor's magnetic axis to cross the previous sector $k - 1$.

The electric angular position can be obtained by numerical integration of (1), applying the constraint that the resulting angular position value has to be within sector k limits. The angular position is, thus, calculated as

$$\begin{aligned} \hat{\theta}_0(t) &= \theta_k + \hat{\omega}_{0k}(t - t_k) \\ \theta_k &\leq \hat{\theta}_0(t) \leq \theta_k + \frac{\pi}{3}. \end{aligned} \quad (3)$$

B. First-Order Algorithm

The rotor speed can be approximated to a better degree by taking into account higher order terms of the Taylor series expansion [7]. The first-order estimation algorithm is given as

$$\omega(t) \cong \hat{\omega}_{1k}(t) = \hat{\omega}_{0k} + \hat{\omega}_{1k}^{(1)}(t - t_k). \quad (4)$$

Fig. 2. Discrete-time vector-tracking observer.

In (4), the first derivative is approximated as

$$\hat{\omega}_{1k}^{(1)} = \frac{\hat{\omega}_{0k} - \hat{\omega}_{0(k-1)}}{\Delta t_{k-1}}. \quad (5)$$

The electric angular position comes out to be

$$\begin{aligned} \hat{\theta}(t) &\cong \hat{\theta}_1(t) = \theta_k + \hat{\omega}_{0k}(t - t_k) + \frac{\hat{\omega}_{1k}^{(1)}}{2}(t - t_k)^2 \\ \theta_k &\leq \hat{\theta}_1(t) \leq \theta_k + \frac{\pi}{3}. \end{aligned} \quad (6)$$

Although it is possible to use higher order approximations, only the first-order one has been considered because of increasing computational times.

C. Vector-Tracking Observer

A different way to approach position estimation is to use a vector-tracking phase-locked loop. The same observer structure has already been used in [9] for Interior PM machine sensorless control. Furthermore, in [10], the vector tracking observer is proposed in order to estimate rotor position from a quantized rotating vector with limited resolution, examining the performance of a low-resolution encoder (1° angular resolution) at steady state. The vector-tracking observer is used here in a new and original fashion; startup and steady-state performances are evaluated, both in simulation and experimentally.

The vector-tracking observer structure, Fig. 2, has two inputs: 1) a rotating vector containing position information and 2) a torque feedforward input to the mechanical model that provides position tracking above the observer bandwidth. The proportional–integral–differential (PID) controller is used to force convergence. A rotating unit-vector based on the observed position is used as feedback to the phase detector. The estimated position is calculated using a latched-torque model of a simple rotational system.

The rotating vector is obtained by processing the sensors' signals. The six possible combinations of the sensors' states

Fig. 3. Stationary reference frame sensors' vector $\vec{H}_{\alpha\beta}$.

can be interpreted as the vertices of a hexagon locus in the stationary reference frame, Fig. 3. Here the rotating vector $\vec{H}_{\alpha\beta}$ is in the 60° position; this means that the rotor magnetic axis is somewhere between 60° and 120° . While the rotor axis crosses a 60° sector, the rotating vector remains in a fixed position, since there are only six possible states.

A consideration of tuning the vector-tracking observer given the quantized nature of the Hall-effect sensors is that the sample rate of the motor position depends on the motor speed. Between transitions of the Hall sensor signal output, the observer relies on the feedforward torque command to estimate the rotor position. If the observer bandwidth is set too high, the resulting position estimate will be quantized. To solve this problem, the observer bandwidth should be speed dependent until a desired bandwidth is attained.

III. STARTUP AND HIGH SPEED CONSIDERATIONS

All three position estimation algorithms can be used only for rotor speeds within a certain range, as described in the following paragraphs.

A. Zeroth- and First-Order Algorithms

The minimum speed ($\omega_{\min}$) is determined by the fact that the initial hypothesis of a constant speed over an entire sector does not hold for very low speeds; added to this is the fact that the velocity may become so low that, in practical digital implementations, the timer used for time measurement overflows before the whole sector is crossed. The maximum speed ($\omega_{\max}$) is determined in theory by the timer's resolution and in practice by the loss of resolution if the speed range becomes too large. In the proposed drive, the minimum speed at which the position estimation algorithm is used has been set to 12 r/min (0.8 Hz supply frequency); the maximum speed has been set to 3000 r/min (200-Hz supply frequency).

As there is a minimum speed under which these estimation algorithms cannot work properly, at startup, a 120° square-wave current control law has been considered to be the most suitable. In [7], it was shown how a bumpless transition between dc brushless and ac brushless modes of operation can be achieved by appropriately choosing the current reference amplitude and the rotor position when the transition occurs.

B. Vector-Tracking Observer

This algorithm does not have the startup problems encountered by the Taylor series algorithms: The drive is started directly in ac brushless mode. Convergence problems cannot arise, since the initial value of $\hat{\theta}$ is set to the value obtained by the low-resolution sensors: The maximum error on the initial angle is, in this way, reduced to 60° and therefore startup is always possible. High speed problems are encountered only above the observer's bandwidth: In this region, the observer behaves as an open-loop observer, being the feedforward signal its only input. This means that the observer will encounter problems in velocity and position estimation if there is an error in the estimated inertia $\hat{J}$. However, assuming that the observer bandwidth and motor motion controller bandwidth are similar, these accuracy errors are above the motor controller bandwidth and have a negligible effect on performance.

IV. SIMULATIONS

Simulations have been carried out with Matlab Simulink to study the behavior of the three position algorithms in the drive's control algorithm. The outer speed loop was tuned to have an 80-Hz bandwidth.

A. Zeroth-Order Estimation Algorithm

Figs. 4 and 5 show the performance of the speed estimation of the zeroth-order estimation algorithm when it is used in the feedback loop of the proposed drive. In particular, Fig. 4 shows the speed transient that follows a step speed command from 0 to 100 rad/s; in accordance with the experimental setup, a linear speed-dependent load is included in the model, so that at 100 rad/s, the motor is working at nominal load conditions. Fig. 5 shows the speed estimation error between the mechanical speed and the estimated speed; a smaller vertical scale has been used in this figure, because the error is small after only 0.5 s

Fig. 4. Mechanical and estimated speed following a step speed command from 0 to 100 rad/s using the zeroth-order algorithm.

Fig. 5. Speed estimation error following a step speed command from 0 to 100 rad/s using the zeroth-order algorithm.

Fig. 6. Electrical and estimated position following a step speed command from zero to 100 rad/s using the zeroth-order algorithm.

from startup. It can be noticed that the error is initially quite large. This is due to the fact that although the speed is low, there is a strong acceleration, so after the first 60° the average velocity is much greater than zero (estimated speed for the first sector); this strong difference between average speed in the previous sector and actual velocity is the cause of the initial error.

Figs. 6 and 7 show the performance of the position estimation. Fig. 6 shows that the acceleration is such that the drive operates in dc brushless mode only in the first sector, since the average speed through the first sector is higher than the 12 r/min

Fig. 7. Position estimation error following a step speed command from 0 to 100 rad/s using the zeroth-order algorithm.

Fig. 8. Mechanical and estimated speed following a step speed command from 0 to 100 rad/s using the first-order algorithm.

transition speed. Also the corrections in the estimated position at the end of each of the first few sectors are visible. This occurs, because the estimated position lags the real position and is therefore corrected at the beginning of a new sector when fresh information is fed to the algorithm from the low-resolution position sensors. As the speed estimation becomes more precise, the position estimation error decreases quickly. After 200 ms, the maximum position estimation error is less than 5.5° , Fig. 7.

B. First-Order Estimation Algorithm

Figs. 8 and 9 show the performance of the speed estimation algorithm when it is used in the feedback loop of the proposed drive. Fig. 8 shows the speed transient that follows the same step speed command as above. Fig. 9 shows the speed estimation error between the mechanical speed and the estimated speed. The error remains initially quite large even with this algorithm, but it decays more quickly and in a smoother way after the first few sectors. The velocity is tracked more precisely, since the estimation now uses also an average acceleration term. After about 120 ms, the speed estimation error is lower than 1 rad/s.

Figs. 10 and 11 show the performance of the position estimation. Fig. 10 shows how the position estimation is more precise than the zeroth-order algorithm; the correction at the end of the sector is practically null after the first two sectors, and can also

Fig. 9. Speed estimation error following a step speed command from 0 to 100 rad/s using the first-order algorithm.

Fig. 10. Electrical and estimated position following a step speed command from zero to 100 rad/s using the first-order algorithm.

Fig. 11. Position estimation error following a step speed command from 0 to 100 rad/s using the first-order algorithm.

be seen in Fig. 11, which shows the error between the actual and estimated position.

C. Vector-Tracking Observer

The observer has been tuned to have the following bandwidths: [80, 2, 0.2] Hz. Fig. 12 shows the speed transient when using the vector-tracking observer. As can be seen in Fig. 2,

Fig. 12. Mechanical and unenhanced observed speed following a step speed command from 0 to 100 rad/s using the vector-tracking observer.

Fig. 13. Enhanced versus un-enhanced speed observation at steady state using the vector-tracking observer.

this observer inherently has two speed signals, namely: 1) the un-enhanced speed signal, which is equal to the integral of the acceleration signal and 2) the enhanced speed signal, which is the sum of the un-enhanced speed signal and the derivative term of controller. Both may be used as the observed speed in the current and speed loops, however, they have different properties. In this application, in which position information has a very low resolution, the different behavior is easily visible at steady state, as shown in Fig. 13. The un-enhanced speed signal is undistinguishable from the speed reference: This is due to the fact that it does not contain the derivative term of the controller. This component, which is present in the enhanced counterpart, is necessary to maintain observer stability. The unenhanced speed signal guarantees a smaller steady-state speed error, albeit at a reduced estimation bandwidth. However, assuming the motion controller and observer are tuned consistently, the ripple of the enhanced estimate does not adversely affect the motion control, but allows for higher disturbance rejection. Fig. 14 shows the speed observation error; it can be noticed that although the error takes longer to reach steady state, compared to the Taylor series algorithms, the error is very small during the initial part of the speed transient: This is due to the phase tracking nature of the observer. The convergence is oscillatory due to two different reasons, namely: 1) the dynamic nature of the observer, which accounts for the slower oscillatory mode

Fig. 14. Speed observation error following a step speed command from 0 to 100 rad/s using the vector-tracking observer.

Fig. 15. Electrical and observed position following a step speed command from 0 to 100 rad/s using the vector-tracking observer.

and 2) the low-resolution position information, which accounts for the higher frequency oscillations.

Fig. 15 shows the performance of the position observation. The observed position initially anticipates the real electrical position and then converges when information from the Hall-effect sensors is obtained; such a behavior is confirmed in Fig. 16 in which the error in position observation oscillates toward a steady state. The reasons for this behavior are the same as for the speed observation.

The vector-tracking observer has by far the best dynamic behavior: Both the maximum errors on speed and position during the rise time are reduced to less than 45% with respect to the Taylor series algorithms.

V. EXPERIMENTAL RESULTS

A drive prototype for home appliance applications, composed of an axial-flux PM machine, a low-cost full-bridge insulated gate bipolar transistor (IGBT) inverter and a 16-bit fixed-point digital signal processor (DSP) in which the aforementioned control algorithm resides, has been built and tested. The adopted axial-flux machine has surface-mounted PM and slotless stator windings; thus its structure is highly isotropic and it exhibits very low inductance, which makes this machine a very good candidate to test the algorithms under

Fig. 16. Position observation error following a step speed command from 0 to 100 rad/s using the vector-tracking observer.

TABLE I
RATED VALUES OF THE MOTOR PROTOTYPE

Rated power	500 W
Rated frequency	200 Hz
Number of poles	8
Rated speed	3000 rpm
Rated voltage	150 V
Rated current	2.24 A
Rated efficiency	90%
Total weight of active parts	0.94 kg

Fig. 17. Prototype axial-flux machine (on the far left) at the test bench.

investigation. In Table I, the main design characteristics of the motor are presented, while Fig. 17 shows the machine at the test bench. The inverter switching frequency is set to 15 kHz and the dead time is $2.5 \mu\text{s}$. An incremental encoder has been mounted on the drive's shaft only to allow a comparison between the estimated angle and a high-resolution measurement. A linear speed-dependent load is coupled to the motor shaft so that at 100 rad/s, the motor is working at nominal load conditions. The following subparagraphs describe the experimental results obtained using all the previously described algorithms.

A. Zeroth-Order Algorithm

Experimental results with the zeroth-order algorithm show a good accordance with the simulations. Fig. 18 shows the position estimation algorithm when the drive is functioning at very low speed. Position correction can be seen at the end of each 60° sector. Position estimation saturation can be seen

Fig. 18. Estimated and measured angular position ($60^\circ/\text{div}$) at near-minimum ac brushless operation speed.

Fig. 19. Estimated angular position and phase current (1 A/vertical div, 5 ms/horizontal div) at rated load torque and 100 rad/s.

toward the end of the third sector: This is due to the fact that the average velocity in the second sector, which is used by the algorithm in the third sector, is higher than the actual average velocity in the third sector, so the estimation algorithm reaches the end of the sector before the physical system. The algorithm corrects itself by saturating its position estimation until a new sector is actually entered.

Fig. 19 shows the performance of the drive at steady state.

B. First-Order Algorithm

Experimental results have shown that the performances of the first-order algorithm are not as satisfactory as simulations predicted. Fig. 20 shows that the estimated angular acceleration given in (5) varies a great deal from one sector to another, even at steady speed; in the drive under test, a periodic nature has been registered in this variation, with a period equal to the mechanical period (four times the electric period). Analysis of this behavior evidenced that the phenomenon is caused by slight differences in the angular width of each sector. Possible reasons for this are Hall-effect sensors hysteresis, imprecise positioning of the sensors, differences in the field produced by adjacent magnets, etc. In this case, even at constant speed,

Fig. 20. Estimated acceleration and estimated speed difference between two adjacent sectors.

Fig. 21. Measured electrical and observed position following a step speed command from 0 to 100 rad/s using the vector-tracking observer (45°/vertical div and 200 ms/horizontal div).

any difference in sector width from the exact 60° causes the estimated acceleration to be different from zero. Most likely, one sector will be bigger and the next one smaller than 60° . Then, the estimated acceleration will switch continuously from negative to positive values, generating a signal affected by a lot of noise. Moreover, it can also be shown that such a noise is proportional to the square of the angular velocity. The angular acceleration signal is too noisy to be employed as it is inside the estimation algorithm. On the other hand, signal filtering cannot be performed, since, otherwise, the effect of the acceleration term will be too slow to be effective. These considerations allow us to conclude that, with low-cost sensors, the first-order algorithm cannot be used, and therefore it is useless to even consider adopting higher order approximations for position estimation.

C. Vector-Tracking Observer

Practical implementation of the vector-tracking observer on the 16-bit DSP included the use of 32-bit arithmetic to be able to obtain sufficient resolution on the controller gains, an important feature in order to guarantee correct dynamic behavior of the observer. However, this did not constitute a problem, since 32-bit arithmetic on a 16-bit processor is a well-known issue and routines that tackle this problem are easily available. In addition, since the programming was done in assembly language, there was no significant problem in computational times, the entire control algorithm being less than $50 \mu\text{s}$, well within the $66.67 \mu\text{s}$ calculation time limit for the 15-kHz pulsewidth modulation (PWM).

The sample time for the observer was set to $266.67 \mu\text{s}$ (3.75 kHz), a compromise between maximum resolution on the position estimation at high speeds and resolution on the observer controller gains. In fact, a lower sample time increases the resolution on position estimation, but in order to obtain the same dynamic performances, the observer gains become smaller. The smaller the gains become, the greater the number of bits necessary to have the desired resolution. However, if precise control at very high shaft speeds (for example, operation well into the field weakening region) is necessary, then the best solution is to use a 32-bit DSP, easily available and at increasingly lower cost, which practically eliminates any type of resolution issues.

Experimental results show very good accordance with simulations. Fig. 21 shows the observer performance at startup; the behavior is the same as predicted in simulation in Fig. 14. A zoom is made at startup to show the actual convergence of the observed position toward the measured position; as can be seen, there is a 30° initial error between the two signals due to the fact that at zero speed, the position is unknown and unobservable. However, both startup in the correct direction and zero steady-state error are achieved. Furthermore, the position observation error shown in Fig. 22 follows closely the simulated behavior in Fig. 15. Fig. 23 shows steady-state performance of the proposed drive when using the vector-tracking observer. The estimated and actual position, the position estimation error and the phase current are shown. It can be seen that correct field orientation is obtained and the average error in position observation is 0° . However, the error presents two types of oscillations, namely: 1) a low-frequency ripple mainly due to the imperfect positioning of the Hall-effect sensors; and 2) a high-frequency ripple (equal to six times the electrical frequency) due to the low-resolution position measurement. In this case, the error in sensor positioning does not affect proper functionality of the observer, thus showing the superiority of this solution to the Taylor algorithms, even regarding sensitivity to sensor misplacement or inaccuracy. Finally, in Fig. 24, the zeroth-order speed estimate and the unenhanced observed speed are compared experimentally, confirming the simulation results shown in Figs. 4 and 12. It can be seen that the unenhanced observed speed is practically a zero-lag filtered version of the speed signal; the first property theoretically descends from the use of the torque feedforward, and the second from the closed-loop nature of the observer. As a confirmation of the first

Fig. 22. Measured position observation error following a step speed command from 0 to 100 rad/s using the vector-tracking observer (15° /vertical div and 200 ms/horizontal div).

Fig. 23. Measured steady state current, measured electrical position, observed position, and position observation error at 100 rad/s (1 A/vertical div, 45° /vertical div, and 5 ms/horizontal div).

property, it can be seen in Fig. 24 that the zeroth-order speed estimate initially lags the unenhanced observed speed; this is due to the fact that in the first sector, the speed is set to zero by the zeroth-order estimation algorithm. The second property is easily confirmed by visual inspection of both signals.

VI. CONCLUSION

In this paper, an innovative brushless ac drive has been presented. Such a drive attempts to overcome some limitations of traditional brushless ac drives concerning the use of high-resolution position sensors. The control algorithm's most innovative feature is its adaptability to the whole speed range including startup. Three different types of speed and position estimation algorithms have been presented and compared theo-

Fig. 24. Zeroth-order speed estimate and unenhanced observed speed following a step speed command from 0 to 100 rad/s (20 rad/s vertical div and 1 s/horizontal div).

retically, in simulation, and experimentally. The experimental results show that when using the vector-tracking observer, the best steady-state and dynamic performances are achieved. Sensor misplacement and inaccuracy is investigated, resulting in the vector-tracking observer yielding the lowest sensitivity. Furthermore, the influence of finite precision calculations and number of bits are considered, and it is shown that, when using a standard fixed-point 16-bit DSP, they do not sensibly influence observer behavior as long as very precise high-speed operation that requires a lower sample period is not necessary. The results are highly satisfactory for the home application that the drive is intended for. Such a drive is ideal in low-cost applications or in any other application that does not require either constant torque at very low speeds or position tracking.

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